

Binomial Distribution Problems

Name: _____

(1) A company owns 400 laptops. Each laptop has an 8% probability of not working. You randomly select 20 laptops for your salespeople.

(a) What is the likelihood that 5 will be broken? (b) What is the likelihood that they will all work?

(c) What is the likelihood that they will all be broken?

$$(1) (a) {}^{20}C_5 (.08)^5 (.92)^{15} = .0145 \quad (b) {}^{20}C_0 (.08)^0 (.92)^{20} = .1887$$

$$(c) {}^{20}C_{20} (.08)^{20} (.92)^0 = .0000000000000000000001 \text{ (note } 2^2 \text{ means move the decimal 22 places to the left)}$$

(2) A study indicates that 4% of American teenagers have tattoos. You randomly sample 30 teenagers. What is the likelihood that exactly 3 will have a tattoo?

$$(2) {}^{30}C_3 (.04)^3 (.96)^{27} = .0863$$

(3) An XYZ cell phone is made from 55 components. Each component has a .002 probability of being defective. What is the probability that an XYZ cell phone will not work perfectly?

$$(3) \text{ Probability that it will work (0 defective components) } {}^{55}C_0 (.002)^0 (.998)^{55} = .896$$

Probability that it will not work perfectly is $1 - .896 = .104$ or 10.4%

(4) The ABC Company manufactures toy robots. About 1 toy robot per 100 does not work. You purchase 35 ABC toy robots. What is the probability that exactly 4 do not work?

$$(4) 35C4 (.01)^4 (.99)^{31} = .00038$$

(5) The LMB Company manufactures tires. They claim that only .007 of LMB tires are defective. What is the probability of finding 2 defective tires in a random sample of 50 LMB tires?

$$(5) 50C2 (.007)^2 (.993)^{48} = .0428$$

(6) An HDTV is made from 100 components. Each component has a .005 probability of being defective. What is the probability that an HDTV will not work perfectly?

$$(6) \text{Probability that it will work (0 defective components) } 100C0 (.005)^0 (.995)^{100} = .606 \text{ Probability that it will not work perfectly is } 1 - .606 = .394 \text{ or } 39.40\%$$